

1st In Semester Examination-2019

B.Com 5th Semester

Subject: Mathematics

Full Marks: 25

Time: 45 Min

Answer any five questions:

1. If the second term and fifth term of an AP are 7 and 19 respectively, find the tenth term and the sum of the first ten terms. 5
2. If a, b, c are the p^{th}, q^{th} and r^{th} terms of a A.P., then show that 5
$$a^{q-r} \cdot b^{r-p} \cdot c^{p-q} = 1$$
3. Solve the following equations: 2+3=5
 - a) $2x^2 - 7x + 6 = 0$
 - b) $x^4 - 10x^2 + 9 = 0$
4. Examine whether the three points (4, 2), (7,5) and (9,7) are collinear or not. 5
5. What is the angle between the lines $x - 2y = 4$ and $y - 3x + 7 = 0$. Also find the slope of the line joining the points (-9, 3) and (-3, 6). 3+2=5
6. Derive an equation of a line in the intercept form. 5
7. (a) What do you mean by a determinant? 2
(b) What do you mean by Cartesian coordinates? 2
(c) Define a rational number. 1
8. (a) Write two properties of a determinant. 2
(b) Prove that:
$$\begin{vmatrix} a & b & c \\ a^2 & b^2 & c^2 \\ a^3 & b^3 & c^3 \end{vmatrix} = abc(a-b)(b-c)(c-a)$$
 3
9. Find the inverse of the following matrix: 5
$$A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 1 \end{bmatrix}$$
10. Solve by Cramer's rule: 5
$$\begin{aligned} 2x + y + z &= 1 \\ x - y + 2z &= -1 \\ 3x + 2y - z &= 4 \end{aligned}$$
11. (a) If $y = f(x) = \frac{x+1}{x+2}$, then what is the value of $f\left(\frac{1}{x}\right)$? 2
(b) Find the value of 3
$$\lim_{x \rightarrow 2} \frac{x^2 - 3x + 2}{x^2 + x - 6}$$
12. Describe in your own words about the importance of calculus in business and commerce. 5